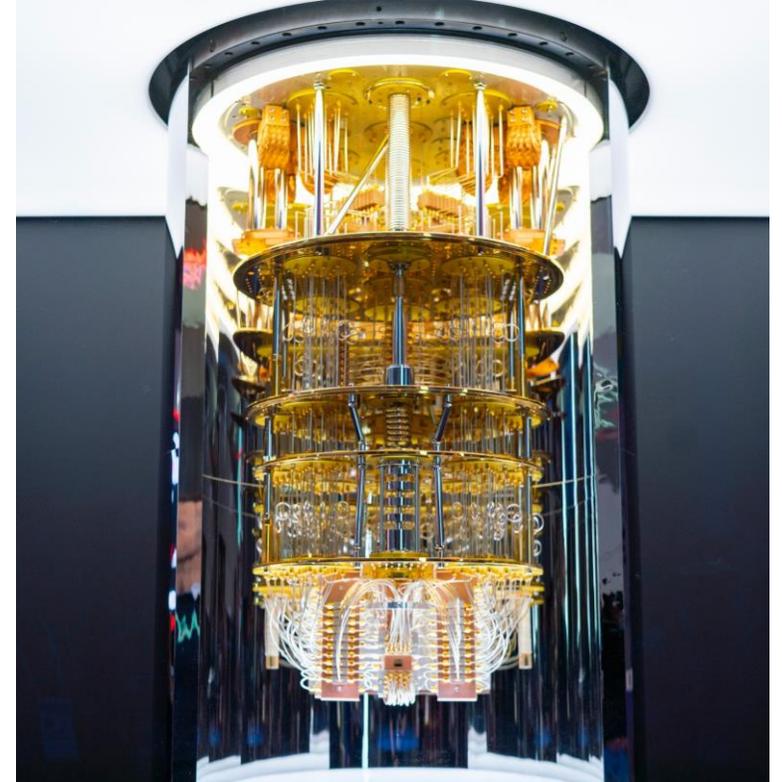


Simulation for (and with) Quantum Computers

Georg Kruse, Simon Mundinar – 12.10.2023 – IISB Annual Symposium 2023

Contents

- 1. Quantum Computer**
 - 1. Qubits: Physical System**
 - 2. Manufacturers**
 - 3. Munich Quantum Valley**
- 2. Simulation for Quantum Computers**
 - 1. Superconducting Qubits**
 - 2. Simulations for Josephson Junctions**
 - 3. Simulation for Control Electronics at Cryogenic Temperatures**
- 3. Simulation with Quantum Computers**
 - 1. Qubits revisited: The Bloch Sphere**
 - 2. What are Quantum Computers good for?**
 - 3. Optimization with Quantum Computers at Fraunhofer IISB**



Part 01



Quantum Computer

Quantum Computer

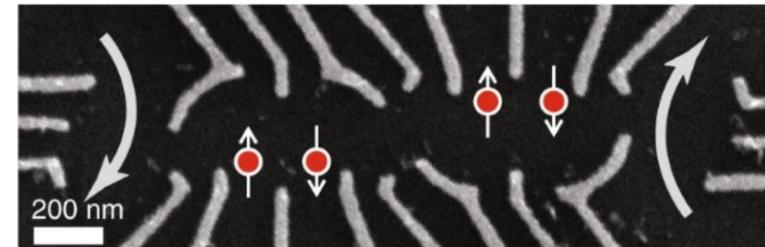
Qubits: Physical System

General Properties

- Any quantum 2-state system can act as a qubit
- However, for useful qubit **additional properties** are necessary:
- **Long relaxation and decoherence times**
 - Lifespan of the qubit's state (e.g., superconducting qubits ~100 μ s; trapped-ion qubits ~10 min)
- **Scalable**
 - One qubit not enough for computing, required are hundreds and more (record: 433 qubits)
- **Controllable**
 - Qubits need to be manipulated and read out, otherwise we cannot do anything
- **Efficiently manufacturable**
 - Ideally no variation between qubits (and cheap production)

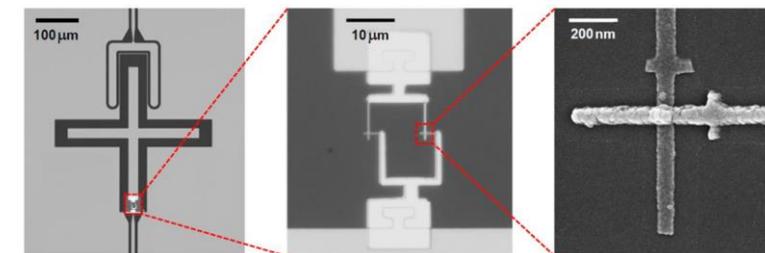
Qubit Architectures

- Huge number of different architectures possible, e.g., color centers, double quantum dots, superconducting circuits, trapped ions, trapped atoms, etc.



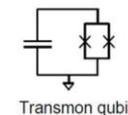
2 double quantum dot qubits

J. M. Nichol, *et al.*, npj Quantum Information **3**, 3 (2017)

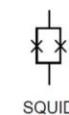


Superconducting Transmon qubit

T. E. Roth, *et al.*, arXiv:2106.11352 (2021)



Transmon qubit



SQUID



Josephson junction

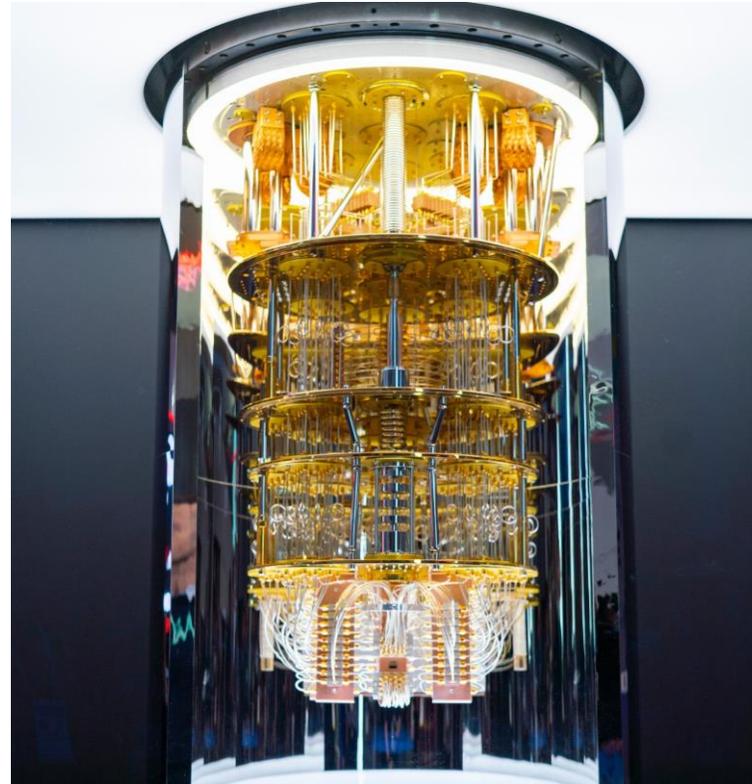
Quantum Computer

Some Manufacturers

IBM Quantum



rigetti



© IBM



D:WAVE

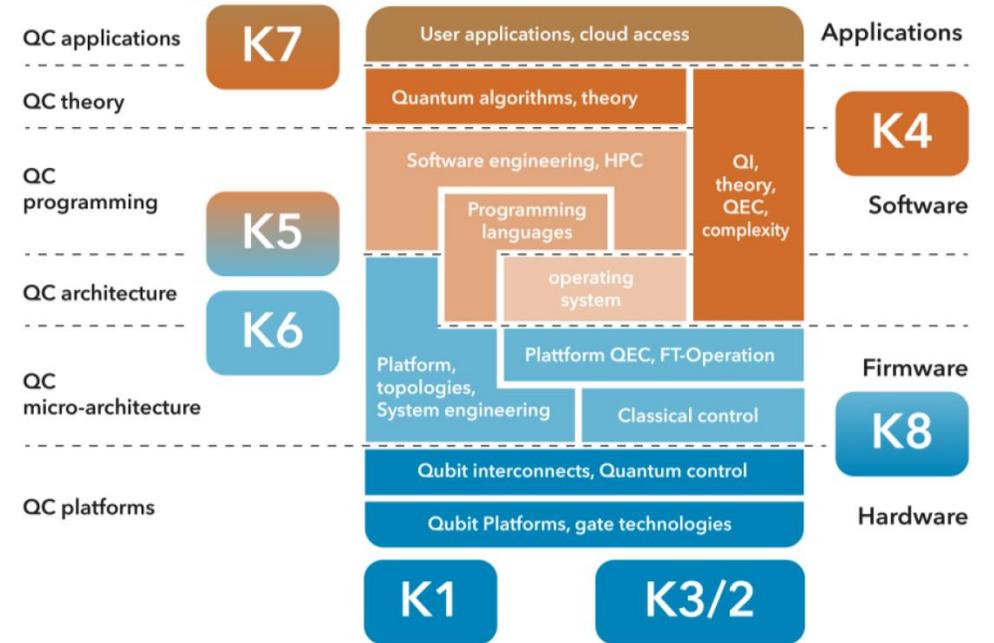
Quantum Computer

Munich Quantum Valley



Building a Bavarian Quantum Computer

- Large Bavarian research project 10/2021 – 09/2026
- From qubit research through integration and application to education
- IISB contributes to consortia
 - K6 "Scalable Hardware & Systems Engineering" (SHARE)
 - K7 "Quantum Algorithms for Application, Cloud & Industry" (QACI)



BAYERISCHE
AKADEMIE
DER
WISSENSCHAFTEN



MAX PLANCK
GESELLSCHAFT



Deutsches Zentrum
für Luft- und Raumfahrt



Friedrich-Alexander-Universität
Erlangen-Nürnberg



LUDWIG-
MAXIMILIANS-
UNIVERSITÄT
MÜNCHEN



Technische
Universität
München

Part 02

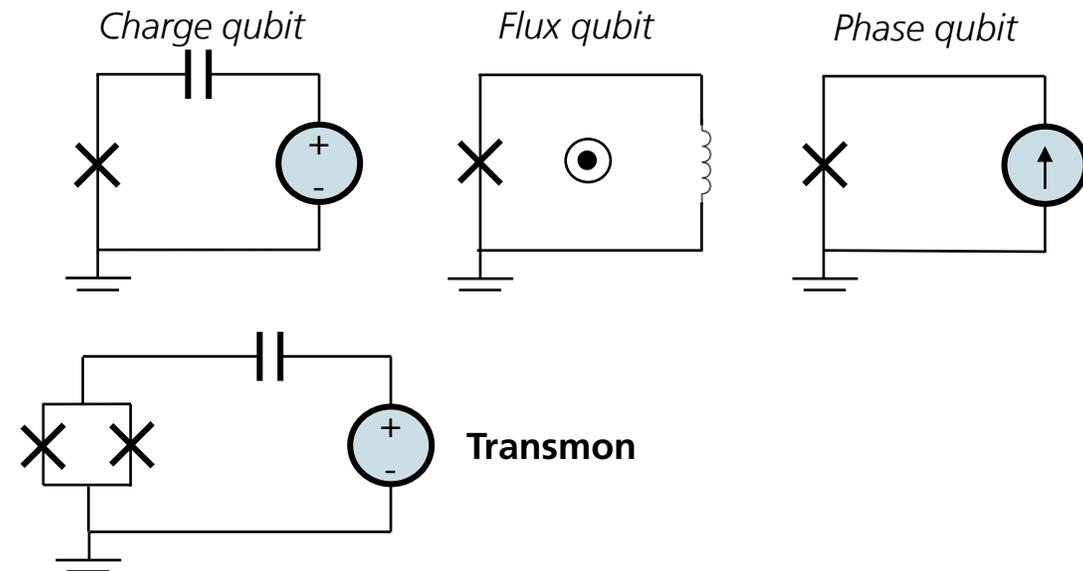
Simulation for Quantum Computers

Simulation for Quantum Computers

Superconducting Qubits

Architectures

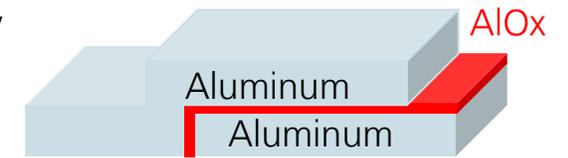
- Several different architectures of superconducting qubits



- Very different physics for different architectures
- All of them based on Josephson junctions

Josephson junctions

- Superconductor-Insulator-Superconductor junctions
- Since superconductors are required, cryogenic temperatures are essential (usually \sim mK)
- **Josephson effect:** Supercurrent through the junction without external voltage
- Electrical transport based on tunneling effect
- Acts as nonlinear inductance, leading to anharmonicity in the oscillator circuits that are the qubits
- Several tasks identified which need simulation support
 - Here 2 examples



Simulation for Quantum Computers

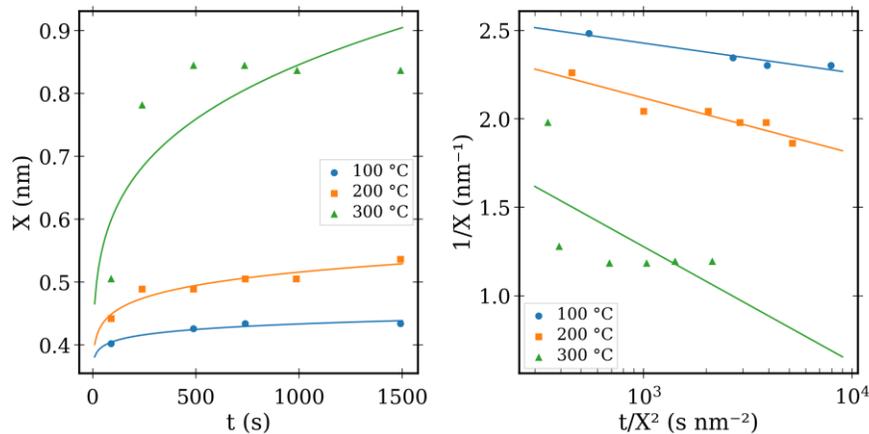
Simulations for Josephson Junctions

Aluminum oxidation

- **Questions:** How does Aluminum oxidize? Are there possibilities to improve the oxidation process?
- Simple model: **Cabrera-Mott theory** with corrections by Ghez [1,2]

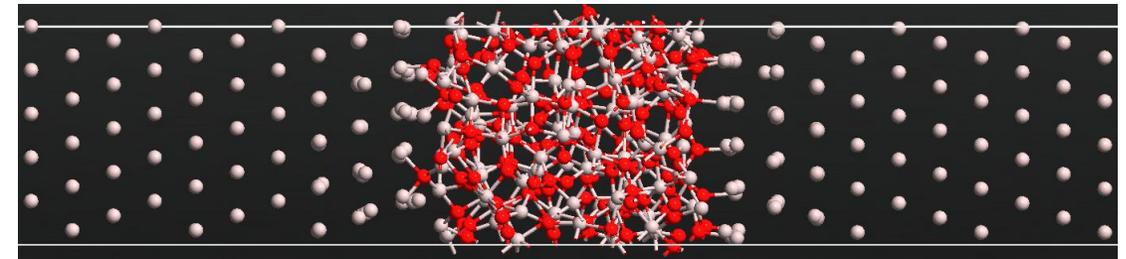
$$\frac{dX}{dt} = 2u \sinh\left(\frac{X_1}{X}\right), \text{ solved by } \frac{1}{X} = -\frac{1}{X_1} \left(\ln \frac{t}{X^2} + \ln X_1 u \right)$$

- **Calibration** based on experimental data from Jeurgens [3]

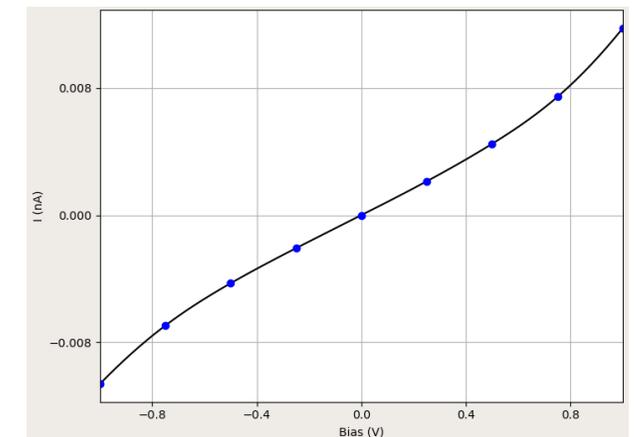


Impact of the oxide

- **Question:** What is the impact of the oxide properties on the current?



- Create oxide with **Molecular Dynamics**
- I(V) curve calculated using **Nonequilibrium Green's Functions Method**
- Differences in the I(V) curve due to oxide stoichiometry
- Also differences due to oxide thickness



[1] N. Cabrera and N. F. Mott, Rep. Prog. Phys. **12**, 163 (1949)

[2] R. Ghez, J. Chem. Phys. **58**, 1838 (1973)

[3] L. P. H. Jeurgens, *et al.*, J. Appl. Phys. **92**, 1649 (2002)

Simulation for Quantum Computers

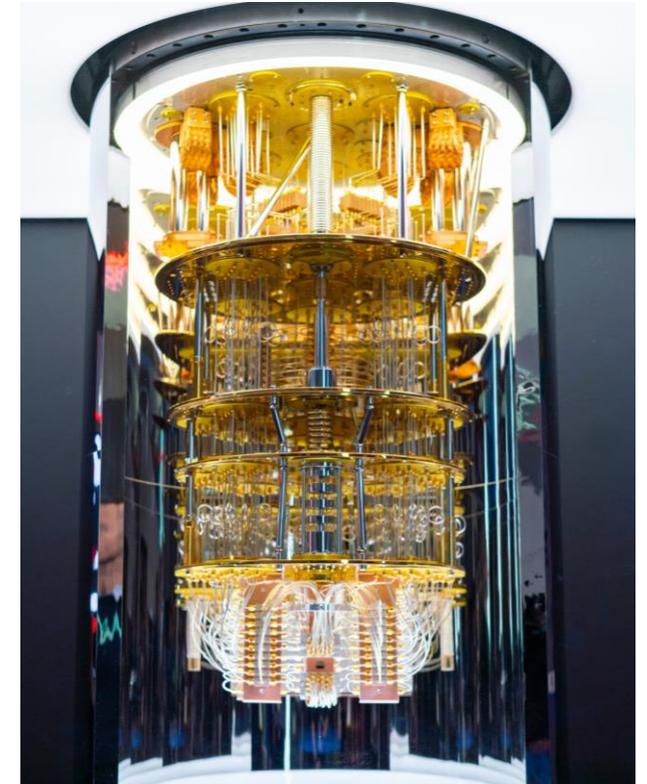
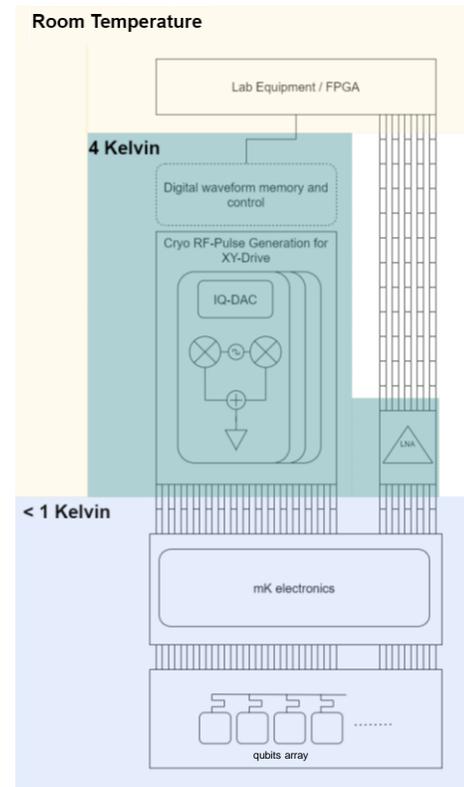
Control Electronics

Controller and Read-out

- Qubits need to be controlled and read-out: Most convenient is electronic read-out
- Controller made in classical electronics: CMOS technology

Temperature strategies

- State-of-the-art quantum computers
 - Qubits at cryogenic temperatures
 - Controller at room temperatures
 - Not scalable system, too many cable connections
- Future quantum computers
 - Qubits and controller at cryogenic temperatures
 - More integrated systems
 - Enable large scale quantum computers



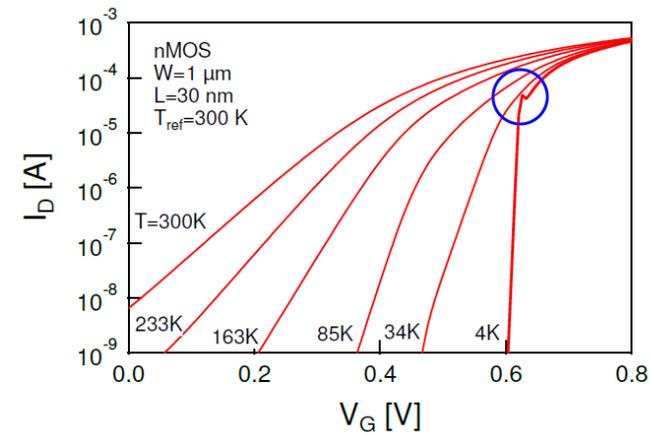
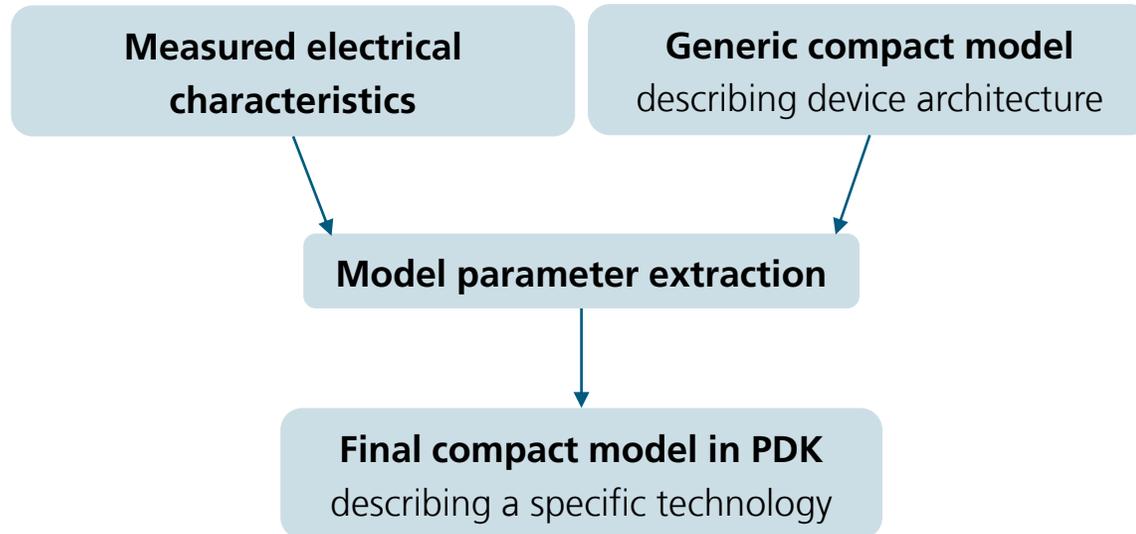
© IBM

Simulation for Quantum Computers

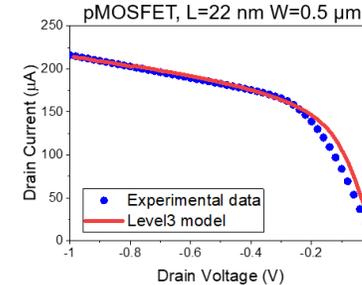
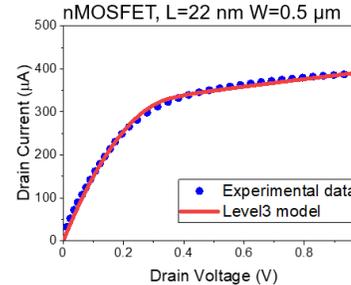
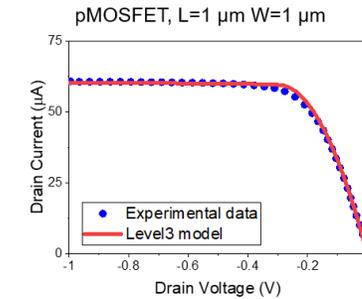
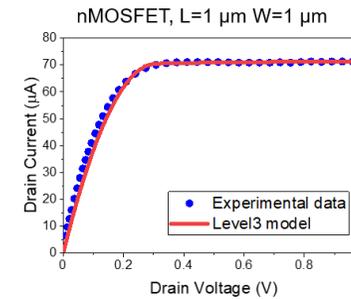
Control Electronics at Cryogenic Temperatures

Transistors at cryogenic temperatures

- Transistors behave differently than at room temperatures
- Current simulation models do not work and need to be adapted
- Design of controller based on simulations of individual transistors
- **Question:** How do transistors behave at cryogenic temperatures?



Conventional models of 28-nm commercial bulk CMOS technology



Some results at T= 3K

Part 03

Simulation with Quantum Computers

Quantum Computing

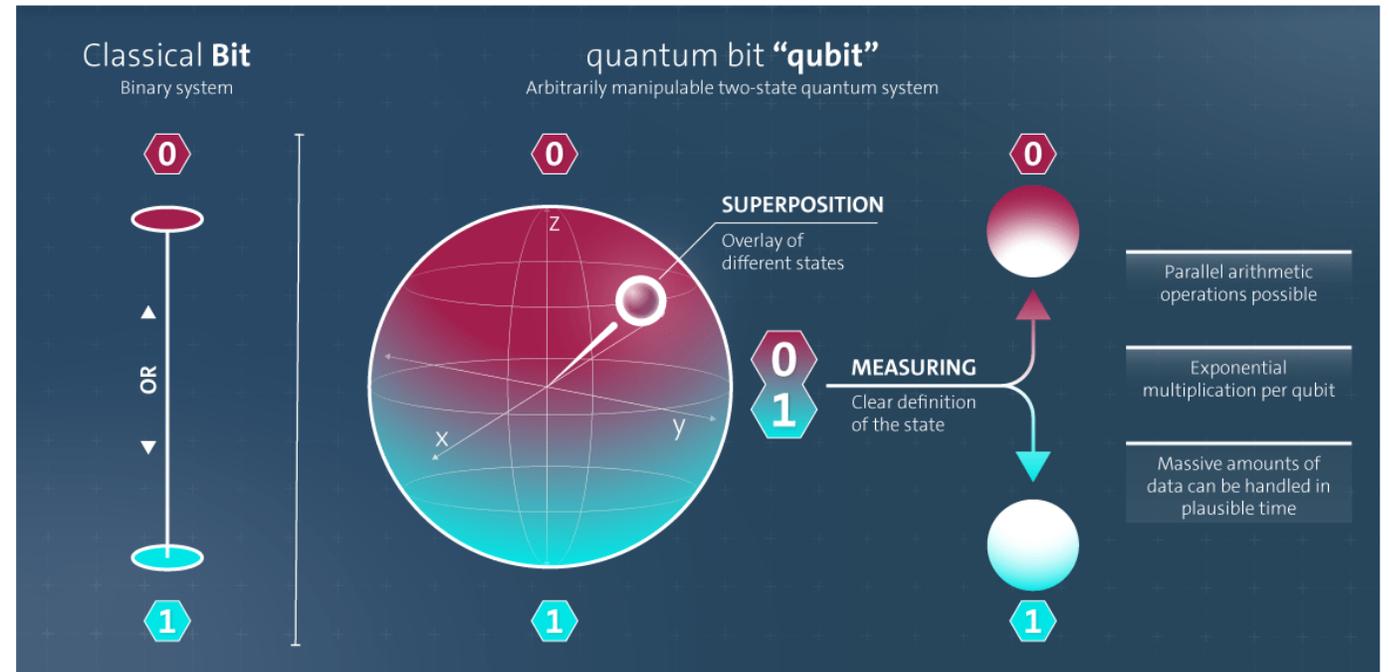
(Logical) Qubits

General Properties

- **Bit:** Classical 2-state system with discrete states (e.g., coin flip)
- **Qubit:** Quantum 2-state system (e.g., spin ½)
- **Superposition:**
 - Qubit can be in any state on Bloch sphere until measured
$$|\psi\rangle = \alpha|0\rangle + \beta|1\rangle$$
 - After measurement: $|\psi\rangle = |0\rangle$ or $|\psi\rangle = |1\rangle$ with probability α^2 and β^2
- **Entanglement:**
 - State space (“information”) scales with 2^n

Scaling Example

- **10 Qubits :** $2^{10} = 1,024$ values
- **100 Qubits:** $2^{100} =$ more values than stars in the known universe

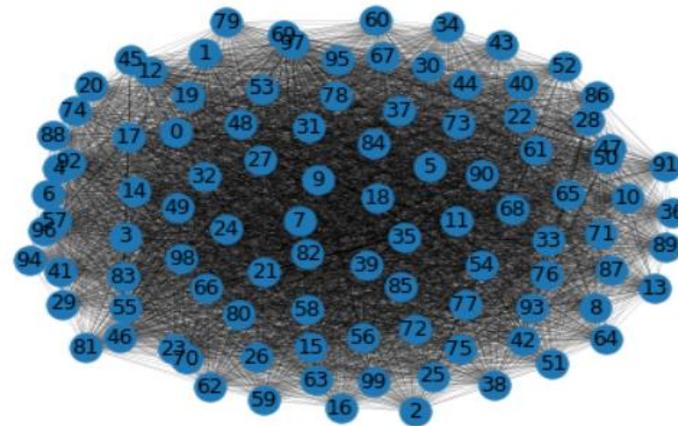


Volkswagen. 2019. "Where is the Electron and How Many of Them?" Volkswagen Group. Accessed 2021-12-27.

Quantum Computing

... and the Curse of Combinatorial Problems

Task: Connect all nodes while minimizing the total length of the edges



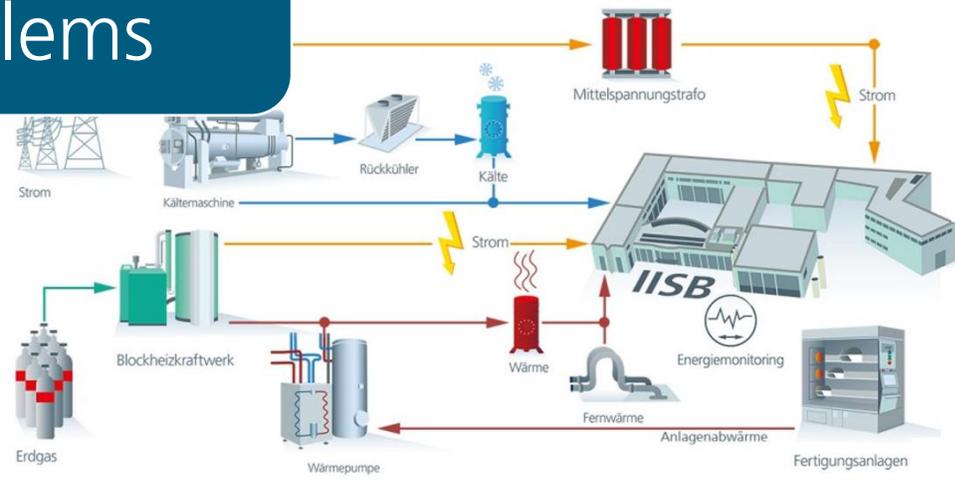
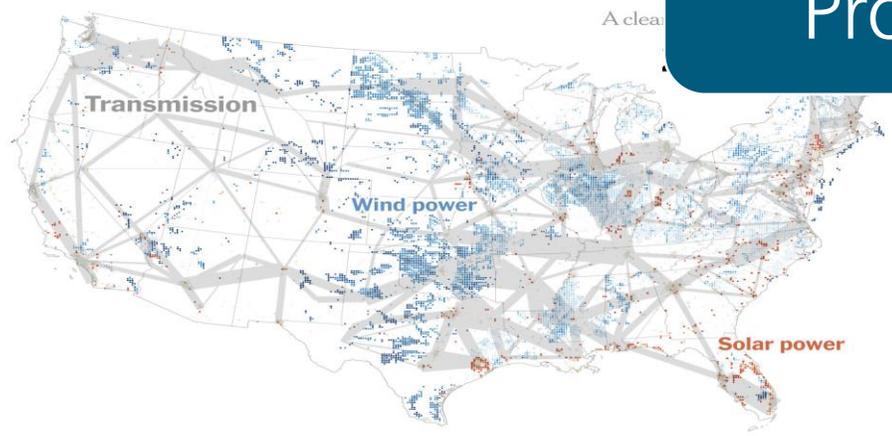
As the number of possible paths grows exponentially with the number of nodes in the graph, quantum advantage is to be expected.

Quantum Computing

Real World Applications



Combinatorial Problems



Quantum Computing at IISB

Quantum Approximate Optimization Algorithm

Unit Commitment Problem

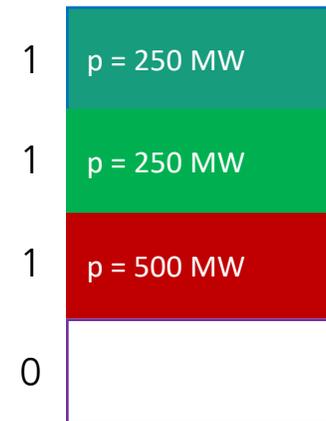
- **Required demand needs to be met** by power plants at each timestep **while minimizing the cost of energy production**
- Mixed Integer Non-Linear Problem
- Classical Solution: MIP Solvers (CPLEX, Gurobi)

Quantum Approximate Optimization Algorithm (QAOA)

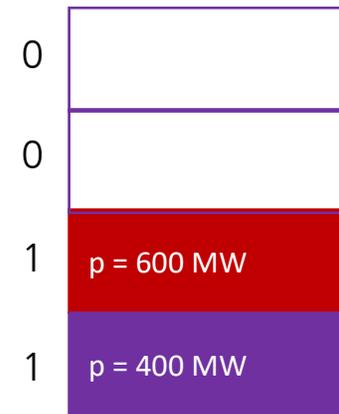
- Each **binary variable** can be encoded into one **qubit**
- Problem is encoded into quantum circuit
- Parameters of quantum circuit are optimized using classical optimizer
- QAOA is a hybrid quantum classical algorithm

4-unit system, $L = 1000$ MW

A = 30\$/h B = 25 \$/MWh C = 100 \$ / MWh ² P _{min} = 100 MW P _{max} = 300 MW	A = 50\$/h B = 10 \$/MWh C = 80 \$ / MWh ² P _{min} = 100 MW P _{max} = 300 MW	A = 20\$/h B = 30 \$/MWh C = 120 \$ / MWh ² P _{min} = 500 MW P _{max} = 900 MW	A = 20\$/h B = 20 \$/MWh C = 70 \$ / MWh ² P _{min} = 0 MW P _{max} = 900 MW
--	---	--	---



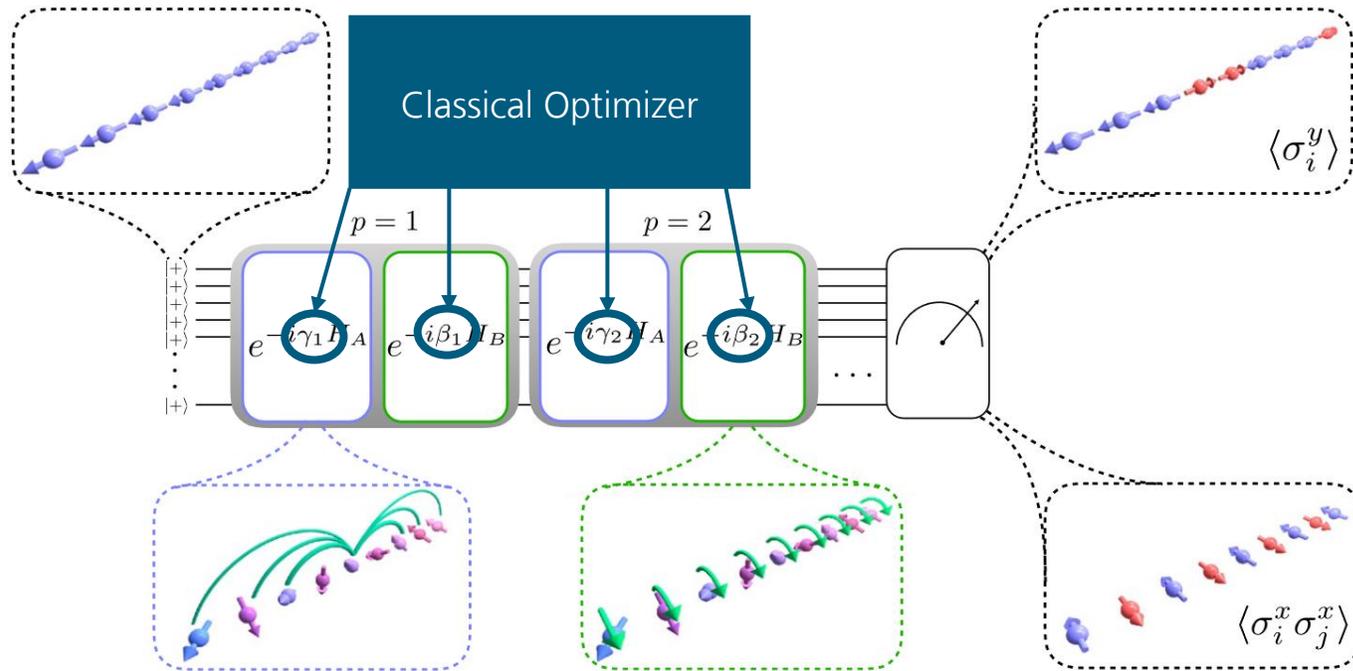
Total cost = $\$4.1 \cdot 10^7$



Total cost = $\$5.4 \cdot 10^7$

Quantum Computing at IISB

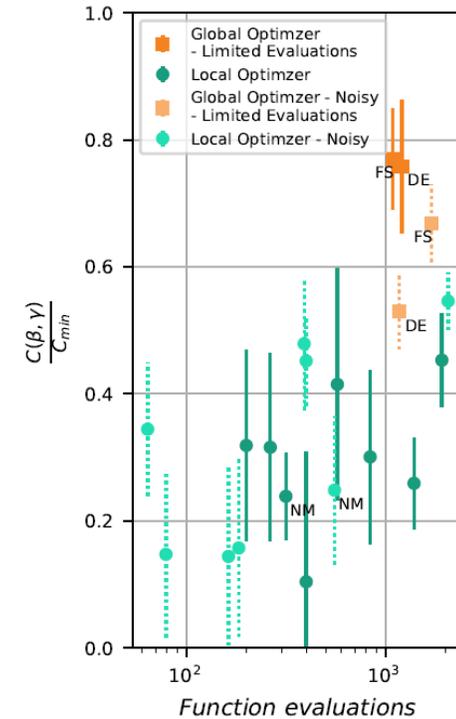
Quantum Approximate Optimization Algorithm



Pagano, Guido, et al. "Quantum approximate optimization of the long-range Ising model with a trapped-ion quantum simulator." *Proceedings of the National Academy of Sciences* 117.41 (2020): 25396-25401.

State of the Art

- Access to 27 Qubit System IBM Q in Ehningen
- Evaluation of classical optimizers for QAOA
- Great difficulties remain **qubit number** and **noise**



Gleißner, Peter, Georg Kruse, and Andreas Roßkopf. "Restricted Global Optimization for QAOA." *arXiv preprint arXiv:2309.12181* (2023).

Thank you for your attention!
